

1. Evaluate the following functions at the given values.

(a) $f(x) = x^2 + 3$; $f(1), f(3), f(4)$

(b) $f(x) = 2x^2 - 5$; $f(-1), f(3), f(4)$

(c) $f(x) = 3x^3$; $f(-3), f(0), f(4)$

(d) $f(x) = 3x^3 - 2x^2$; $f(1), f(2), f(3)$

(e) $g(x) = \frac{x}{4}$; $g(0), g(6), g(9)$

(f) $g(x) = \frac{3x + 7}{4}$; $g(-2), g(0), g(8)$

(g) $h(t) = \frac{t}{t+1}$; $h\left(\frac{4}{3}\right), h\left(\frac{1}{3}\right), h\left(\frac{5}{3}\right)$

(h) $h(t) = \frac{t+1}{t-1}$; $h\left(\frac{3}{2}\right), h\left(\frac{1}{2}\right), h\left(\frac{1}{4}\right)$

2. Evaluate at the given values.

(a) $f(x) = \frac{1-3x}{2}$; $f(-2), f(a), f(-a), f(a-1)$

(b) $f(t) = t + \frac{3}{t}$; $f(3), f(1/3), f(x-1), f\left(\frac{1}{x}\right)$

(c) $f(t) = \sqrt{2+3t}$; $f(5), f(a), f(x+h)$

(d) $f(x) = \frac{1}{1+x}$; $f\left(\frac{1}{2}\right), f(x+2), f(x+h)$

(e) $f(x) = 3|x-2|$; $f(-2), f\left(\frac{1}{2}\right), f(x+1), f(x^2+2)$

(f) $f(x) = \frac{1}{x^2}$; $f\left(\frac{1}{2}\right), f(-1), f(x+h)$

(g) $f(x) = 3$; $f(2), f\left(\frac{1}{2}\right), f(x+h)$

(h) $f(x) = \frac{2}{x^2+1}$; $f\left(-\frac{1}{3}\right), f(a), f(x+h)$

(i) $f(x) = \frac{1}{\sqrt{3x-5}}$; $f(2), f(z), f(x+h)$

3. Find $\frac{f(x+h) - f(x)}{h}$. Simplify as in the videos.

(a) $f(x) = \sqrt{2+3x}$

(b) $f(x) = \frac{1}{1+x}$

(c) $f(x) = \frac{1}{x^2}$

(d) $f(x) = \frac{2}{x^2+1}$

(e) $f(x) = \frac{1}{\sqrt{x}}$

(f) $f(x) = \frac{1}{\sqrt{3x-5}}$

4. Find the x and y -intercepts of the following functions.

(a) $f(x) = 3x + 5$

(b) $f(x) = 1 - 2x$

(c) $f(x) = |x - 2|$

(d) $f(x) = |2x - 3| - 1$

(e) $f(x) = x^3 - 27$

(f) $f(x) = 16 - x^2$

(g) $f(x) = x^3 + 125$

(h) $f(x) = x^2 - x - 2$

(i) $f(x) = x^3 - x$

(j) $f(x) = 8x - x^4$

(k) $f(x) = x^2 - 5x - 14$

(l) $f(x) = 8 - x^2$

Answers

1. (a) 4, 12, 19 (b) -3, 13, 27 (c) -81, 0, 192 (d) 1, 16, 63
 (e) $0, \frac{3}{2}, \frac{9}{4}$ (f) $\frac{1}{4}, \frac{7}{4}, \frac{31}{4}$ (g) $\frac{4}{7}, \frac{1}{4}, \frac{5}{8}$ (h) 5, -3, $-\frac{5}{3}$
2. (a) $\frac{7}{2}, \frac{1-3a}{2}, \frac{1+3a}{2}, \frac{4-3a}{2}$ (b) $4, \frac{28}{3}, \frac{x^2-2x+4}{x-1}, \frac{1+3x^2}{x}$
 (c) $\sqrt{17}, \sqrt{2+3a}, \sqrt{2+3(x+h)}$ (d) $\frac{2}{3}, \frac{1}{x+3}, \frac{1}{1+x+h}$
 (e) $12, \frac{9}{2}, 3|x-1|, 3x^2$ (f) $4, 1, \frac{1}{(x+h)^2}$
 (g) 3, 3, 3 (h) $\frac{9}{5}, \frac{2}{a^2+1}, \frac{2}{(x+h)^2+1}$
 (i) $1, \frac{1}{\sqrt{3z-5}}, \frac{1}{\sqrt{3(x+h)-5}}$
3. (a) $\frac{3}{\sqrt{2+3(x+h)} + \sqrt{2+3x}}$ (b) $\frac{-1}{(1+x)(1+x+h)}$
 (c) $\frac{-(2x+h)}{x^2(x+h)^2}$ (d) $\frac{-4x-2h}{((x+h)^2+1)(x^2+1)}$
 (e) $\frac{-1}{\sqrt{x(x+h)}(\sqrt{x} + \sqrt{x+h})}$
 (f) $\frac{-3}{\sqrt{(3x-5)(3(x+h)-5)}(\sqrt{3x-5} + \sqrt{3(x+h)-5})}$
4. (a) x -intercept: $-5/3$, y -intercept: 5 (b) x -intercept: $1/2$, y -intercept: 1
 (c) x -intercept: 2, y -intercept: 2 (d) x -intercepts: 1, 2, y -intercept: 2
 (e) x -intercept: 3, y -intercept: -27 (f) x -intercepts: -4, 4, y -intercept: 16
 (g) x -intercept: -5, y -intercept: 125 (h) x -intercepts: -1, 2, y -intercept: -2
 (i) x -intercepts: -1, 0, 1, y -intercept: 0 (j) x -intercepts: 0, 2, y -intercept: 0
 (k) x -intercepts: -2, 7, y -intercept: -14 (l) x -intercepts: $-2\sqrt{2}, 2\sqrt{2}$, y -intercept: 8